



National 5 Mathematics

Pythagoras' Theorem – Solutions

Marks are indicated in brackets after each question number

2014 Paper 2 Question 6, (4)

Since Lowtown is due west of Midtown then Hightown can only be directly north of Lowtown if the triangle is right-angled.

Let H = Hightown, L = Lowtown, M= Midtown

$$\text{Then } (LH)^2 + (LM)^2 = 85^2 + 75^2 = 12,850$$

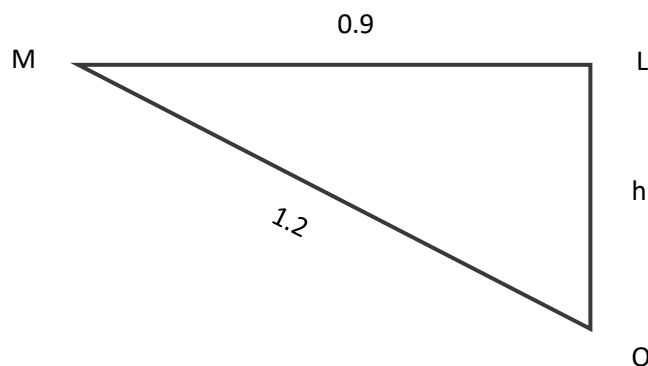
$$(HM)^2 = 110^2 = 12,100$$

Since $(LH)^2 + (LM)^2 \neq (HM)^2$ the triangle is not right-angled.

Therefore, Hightown is not directly north of Lowtown.

2015 Paper 2 Question 12, (4)

Construct a right triangle from the midpoint of ML with O & M.



Using Pythagoras gives

$$1.2^2 = 0.9^2 + h^2$$

Solving gives $h = 0.79 \text{ m}$

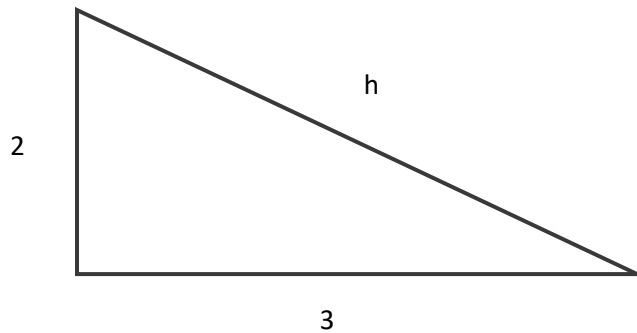
So, depth of milk = $0.79 + \text{radius} = 0.79 + 1.2 = 2.78 \text{ m}$.

2016 Paper 1 Question 7, (4)

a) $B = (8, 4, 0)$ by inspection of the graph.



b) Create a right-angled triangle in the base.



Using Pythagoras, we have

$$h = \sqrt{2^2 + 3^2} = \sqrt{13}$$

$$(AV)^2 = 6^2 + (\sqrt{13})^2$$

$$= 49$$

$$AV = 7$$

2016 Paper 2 Question 16, (4)

Construct a right-angled triangle with long side 6.6 cm and a short side of 4.5 cm.

Using Pythagoras, we have

$$b^2 + 4.5^2 = 6.6^2$$

$$b^2 = 6.6^2 - 4.5^2$$

$$b^2 = 23.31$$

$$b = \sqrt{23.31} = 4.8 \text{ cm}$$

$$\text{Height} = 4.8 + \text{radius}$$

$$= 4.8 + 6.6$$

$$= 11.4 \text{ cm}$$

**2017 Paper 2 Question 7, (3)**

The hypotenuse of the larger triangle is 22 cm.

The short sides have length 8 cm and 19 cm.

$$8^2 + 19^2 = 425$$

$$22^2 = 484$$

Since $425 \neq 484$ the triangle is not right angled by the converse of Pythagoras.

2018 Paper 2 Question 12, (4)

Let M be the mid-point of AB.

Construct a right-angled triangle OAM.

Using Pythagoras, $13^2 - 10^2 = 169 - 100 = 69$.

$$\sqrt{69} = 8.3$$

$$\text{Width} = \text{Radius} + 8.3 = 13 + 8.3 = 21.3 \text{ cm.}$$

2019 Paper 2 Question 11, (4)

The length of B to C is given by $1500 - 600 - 650 = 250 \text{ m}$.

$$650^2 = 422,500$$

$$600^2 + 250^2 = 422,500$$

Since $600^2 + 250^2 = 650^2$ a triangle with short sides 600 & 250 and long side 650 is a right-angled triangle by the Converse of Pythagoras' Theorem.

So, ABC is a right-angled triangle, meaning that B is due east of A since C is due north of B.

2019 Paper 2 Question 18, (4)

Create a right angled triangle TSB.

Since TS & SB are the radius of the circle they have length 7.5 cm.

$$\begin{aligned} \text{By Pythagoras, } TB &= \sqrt{7.5^2 + 7.5^2} \\ &= 10.6 \text{ cm} \end{aligned}$$

TB is the radius of the larger circle, so TD also has length 10.6 cm.

So, height = $10.6 + 15 = 25.6 \text{ cm}$.



2022 Paper 2 Question 8, (4)

Set up a right angled triangle with long side = 2.9 m and short side = 2 m.

By Pythagoras we have

$$a^2 + 2^2 = 2.9^2$$

$$a^2 + 4 = 8.41$$

$$a^2 = 4.41$$

$$a = \sqrt{4.41} = 2.1$$

$$\text{Height} = 2.1 + \text{radius}$$

$$= 2.1 + 2.9 = 5m$$

2022 Paper 2 Question 11, (3)

Set up a right angled triangle on the base of the cuboid, EGH .

This triangle has short sides 24 cm and 6 cm. Let the long side be c .

Using Pythagoras gives

$$24^2 + 6^2 = c^2$$

$$576 + 36 = c^2$$

$$c^2 = 612$$

$$c = 24.7 \text{ cm}$$

Set up a second right angled triangle which includes the diagonal, ECC .

This triangle has short sides 24.7 cm and 8 cm. Let the long side be c .

Using Pythagoras gives

$$24.7^2 + 8^2 = c^2$$

$$610.1 + 64 = c^2$$

$$c^2 = 674.1$$

$$c = 26 \text{ cm}$$



2023 Paper 1 Question 10, (4)

Consider a right angled triangle from the midpoint of AB to A to C.

This triangle has a short side of 30 *cm*, and a long side of 50 *cm*. Let the other short side be *a*. Then, using Pythagoras we have,

$$a^2 + 30^2 = 50^2$$

$$a^2 + 900 = 2500$$

$$a^2 = 1600$$

$$a = 40 \text{ cm}$$

So, the width = 40 + *radius*

$$= 40 + 50$$

$$= 90 \text{ cm}$$

2023 Paper 2 Question 8, (4)

The wall is perpendicular (i.e. right-angled) to the ground if the triangle *ABC* is right-angled.

$$4^2 + 7^2 = 16 + 49 = 65$$

$$8^2 = 64$$

Since $65 \neq 64$, by the converse of Pythagoras Theorem, the triangle is not right-angled.

Therefore, the wall is not perpendicular to the ground.

2024 Paper 2 Question 10, (4)

Set up a right-angled triangle between A, C and the mid-point of A and B.

This triangle has side lengths 10 *cm* and 7.5 *cm* and we use Pythagoras to find the length of the other side (the mid-point of AB to C).

Using Pythagoras gives:

$$\sqrt{10^2 - 7.5^2} = 6.6$$

So the length of the mid-point of AB to C is 6.6 *cm*

The total width is $(2 \times 6.6) + (2 \times \text{the radius})$

$$= (2 \times 6.6) + (2 \times 10)$$

$$= 33.2 \text{ cm}$$



2025 Paper 2 Question 8, (1) (3)

a) $M = (4, 3, 12)$

b) Construct a right-angled triangle on the base, OQR .

Using Pythagoras $OQ = \sqrt{3^2 + 4^2} = 5$

Construct a right-angled triangle OQM

Using Pythagoras $OM = \sqrt{5^2 + 12^2} = 13$

So, OM has length 13 units.