## National 5 Mathematics

## Simultaneous Equations - Solutions

Marks are indicated in brackets after each question number

## 2014 Paper 2 Question 3, (2)

a) $5 a+3 c=158.25$
b) $3 a+2 c=98$
c) $5 a+3 c=158.25$
$3 a+2 c=98$

Multiplying (1) by 2 and (2) by 3 gives
$10 a+6 c=316.5$
$9 a+6 c=294$
(3) - (4) gives
$a=316.5-294=22.5$
Substituting into (2) gives
$(3 \times 22.5)+2 c=98$
$c=15.25$

So, an adult ticket costs $£ 22.50$ and a child ticket costs $£ 15.25$.

## 2015 Paper 1 Question 11, (3)

$3 x+2 y=17$
$2 x+5 y=4$

Multiply (1) by 2 and (2) by 3 to give
$6 x+4 y=34$
$6 x+15 y=12$
(4) - (3) gives
$11 y=-22$
$y=-2$

Substituting $y=-2$ into (2) gives
$2 x+5 \cdot(-2)=4$
$2 x-10=4$
$2 x=14$
$x=7$

2016 Paper 1 Question 4, (1) (1) (4)
a) $2 c+3 d=9.6$
b) $3 c+4 d=13.3$

$$
\text { c) } \begin{align*}
2 c+3 d & =9.6  \tag{1}\\
3 c+4 d & =13.3 \tag{2}
\end{align*}
$$

Multiply (1) by 3 and (2) by 2 to give
$6 c+9 d=28.8$
$6 c+8 d=26.6$
(3) - (4) gives
$d=2.2$

Substitute $d=2.2$ into (1) to give
$2 c+(3 \times 2.2)=9.6$
$2 c+6.6=9.6$
$2 c=3$
$c=1.5$

Dress requires $2.2 \mathrm{~m}^{2}$ and cloak requires $1.5 \mathrm{~m}^{2}$.

## 2017 Paper 1 Question 13, (3)

$$
\begin{equation*}
3 x-y=2 \tag{1}
\end{equation*}
$$

$x+3 y=19$

Multiplying (1) by three gives
$9 x-3 y=6$
$x+3 y=19$
$(3)+(2)$ gives
$10 x=25$
$x=2.5$

Substitute $x=2.5$ into (1) to give
(3 $x 2.5$ ) $-y=2$
$7.5-y=2$
$y=5.5$

So, $\mathrm{P}=(2.5,5.5)$.

## 2018 Paper 1 Question 3, (3)

$$
\begin{align*}
& 4 x+5 y=-3  \tag{1}\\
& 6 x-2 y=5 \tag{2}
\end{align*}
$$

Multiply (1) by 2 and multiply (2) by 5 to give

$$
\begin{equation*}
8 x+10 y=-6 \tag{3}
\end{equation*}
$$

$30 x-10 y=25$
$(3)+(4)$ gives
$38 x=19$
$x=0.5$

Substitute $x=0.5$ into (1) to give

$$
\begin{aligned}
4 \times 0.5+5 y & =-3 \\
2+5 y & =-3 \\
5 y & =-5, y=-1
\end{aligned}
$$

2019 Paper 1 Question 8, (1) (1) (4)
a) $7 c+3 g=215$
b) $5 c+4 g=200$

$$
\text { c) } \begin{align*}
7 c+3 g & =215  \tag{1}\\
5 c+4 g & =200 \tag{2}
\end{align*}
$$

Multiply (1) by 4 and multiply (2) by 3 to give

$$
\begin{align*}
& 28 c+12 g=860  \tag{3}\\
& 15 c+12 g=600 \tag{4}
\end{align*}
$$

(3) - (4) gives
$13 c=260$
$c=20$

2022 Paper 2 Question 4, (1) (1) (4)
a) $4 m+3 a=4.25$
b) $5 m+2 a=4.70$
c) $4 m+3 a=4.25$
$5 m+2 a=4.70$
Multiply (1) by 2 and (2) by 3 to give

$$
\begin{equation*}
8 m+6 a=8.5 \tag{3}
\end{equation*}
$$

$15 m+6 a=14.1$
(4) - (3) gives
$7 m=5.6$
$m=0.8$

Substitute $m=0.8$ into (1) to give
$4(0.8)+3 a=4.25$
$3.2+3 a=4.25$
$3 a=1.05$
$a=0.35$

So, a mango costs 80 p and an apple costs 35 p.

## 2023 Paper 1 Question 3, (3)

$$
\begin{equation*}
2 x+3 y=8 \tag{1}
\end{equation*}
$$

$5 x+2 y=-2$

Multiply (1) by 2 and multiply (2) by 3 to give

$$
\begin{align*}
& 4 x+6 y=16  \tag{3}\\
& 15 x+6 y=-6 \tag{4}
\end{align*}
$$

(4) - (3) gives
$11 x=-22$
$x=-2$

Substitute $x=-2$ into (1) to give
$2(-2)+3 y=8$
$-4+3 y=8$
$3 y=12$
$y=4$

