



## 2019 National 5 Mathematics Paper 1

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### Question 1, (2)

$$f(x) = 5x^3$$

$$f(-2) = 5 \cdot (-2)^3$$

$$= 5 \cdot -8$$

$$= -40$$

### Question 2, (2)

$$\frac{3}{8} \times 1\frac{5}{7} = \frac{3}{8} \times \frac{12}{7}$$

$$= \frac{36}{56}$$

$$= \frac{9}{14}$$

### Question 3, (3)

$$(x + 5)(2x^2 - 7x - 3)$$

$$= 2x^3 - 7x^2 - 3x + 10x^2 - 35x - 15$$

$$= 2x^3 + 3x^2 - 38x - 15$$

### Question 4, (3)

$$\text{Arc Length} = \frac{\text{angle}}{360} \times \pi \times d$$

$$= \frac{240}{360} \times 3.14 \times 60$$

$$= \frac{2}{3} \times 3.14 \times 60$$

$$= 40 \times 3.14$$

$$= (40 \times 3) + (40 \times 0.1) + (40 \times 0.04)$$

$$= 120 + 4 + 1.6$$

$$= 125.6 \text{ cm}$$



### Question 5, (3) (2)

a) Reordering gives

3 3 4 4 5 6 7 9 10

Median = 5

$Q_3 = 8$

$Q_1 = 3.5$

$$\text{Semi-IQR} = \frac{8 - 3.5}{2} = \frac{4.5}{2} = 2.25$$

b) The median temperature was higher in Endoch than Grantford meaning that on average Endoch had higher midday temperatures over the nine day period.  
The semi-interquartile range was lower in Endoch than Grantford meaning that the temperatures recorded over the nine day period were more consistent there.

### Question 6, (3) (1)

a) Choose two points that lie on the line of best fit, (1.5, 14), (3.5, 8).

$$\begin{aligned}\text{Gradient} &= \frac{14 - 8}{1.5 - 3.5} \\ &= \frac{6}{-2} \\ &= -3\end{aligned}$$

Using  $y - b = m(x - a)$  with (1.5, 14) gives

$$y - 14 = -3(x - 1.5)$$

$$y - 14 = -3x + 4.5$$

$$y = -3x + 18.5$$

$$F = -3E + 18.5$$

b) Substituting  $E = 1.1$  gives

$$F = (-3 \times 1.1) + 18.5$$

$$= -3.3 + 18.5$$

$$= 15.2$$

15.2 Kilometres per litre.



**Question 7, (3)**

$$A = \frac{1}{2}h(x + y)$$

$$2A = h(x + y)$$

$$2A = hx + hy$$

$$2A - hy = hx$$

$$x = \frac{2A - hy}{h}$$

**Question 8, (1) (1) (4)**

a)  $7c + 3g = 215$

b)  $5c + 4g = 200$

c)  $7c + 3g = 215$  (1)

$$5c + 4g = 200 \quad (2)$$

Multiply (1) by 4 and multiply (2) by 3 to give

$$28c + 12g = 860 \quad (3)$$

$$15c + 12g = 600 \quad (4)$$

(3) - (4) gives

$$13c = 260$$

$$c = 20$$

**Question 9, (1) (1) (1)**

a)  $x = 4$

b) i)  $a = -4$

ii)  $b = 20$

**Question 10, (1) (2)**

a)  $\overrightarrow{PQ} = \overrightarrow{PR} + \overrightarrow{RQ}$

$$= \begin{pmatrix} 6 \\ -4 \end{pmatrix} + \begin{pmatrix} -1 \\ 8 \end{pmatrix} = \begin{pmatrix} 5 \\ 4 \end{pmatrix}$$



$$\begin{aligned}\text{b) } \overrightarrow{MQ} &= \overrightarrow{MP} + \overrightarrow{PQ} \\ &= \frac{1}{2}\overrightarrow{RP} + \overrightarrow{PQ} \\ &= -\frac{1}{2}\overrightarrow{PR} + \overrightarrow{PQ} \\ &= -\frac{1}{2}\begin{pmatrix} 6 \\ -4 \end{pmatrix} + \begin{pmatrix} 5 \\ 4 \end{pmatrix} \\ &= \begin{pmatrix} -3 \\ 2 \end{pmatrix} + \begin{pmatrix} 5 \\ 4 \end{pmatrix} \\ &= \begin{pmatrix} 2 \\ 6 \end{pmatrix}\end{aligned}$$

### Question 11, (3)

All of the angles at  $O = 360 \div 5 = 72^\circ$

$$AOB = 72^\circ$$

$$FOB = 180 - 72 = 108^\circ$$

$$OFB = \frac{180 - 108}{2} = 36^\circ$$

### Question 12, (3)

$$\frac{\sqrt{2}}{\sqrt{40}} = \frac{\sqrt{2}}{\sqrt{2}\sqrt{20}} = \frac{1}{\sqrt{20}} = \frac{1}{\sqrt{20}} \times \frac{\sqrt{20}}{\sqrt{20}} = \frac{\sqrt{20}}{20} = \frac{\sqrt{4}\sqrt{5}}{20} = \frac{2\sqrt{5}}{20} = \frac{\sqrt{5}}{10}$$

### Question 13, (2)

$$x - \text{co-ordinate of } A = 180 - 45 = 135$$

$$y - \text{co-ordinate of } A = -1 \times 3 = -3$$

Co-ordinates of  $A = (135, -3)$ .

### Question 14, (3)

$$\frac{x}{2} - 1 = \frac{3 - x}{5}$$

Multiply through the equation by 10 to give

$$\frac{10x}{2} - 10 = \frac{30 - 10x}{5}$$

$$5x - 10 = 6 - 2x$$

$$7x = 16$$

$$x = \frac{16}{7}$$



**Question 15, (1) (4)**

**a)**  $h = 12t - 5t^2$

Substitute  $t = 2$  to give

$$h = (12 \times 2) - 5(2^2)$$

$$= 24 - 20$$

$$= 4$$

4 metres

**b)** Substitute  $h = -17$  to give

$$-17 = 12t - 5t^2$$

$$5t^2 - 12t - 17 = 0$$

$$(5t - 17)(t + 1) = 0$$

$$5t - 17 = 0$$

$$t = \frac{17}{5}$$

$$t = 3.4$$

$$t + 1 = 0$$

$$t = -1$$

Since  $t$  represents *time* this solution can be discarded.

So, the ball will hit the sea after 3.4 seconds.



## 2019 National 5 Mathematics Paper 2

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1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19

### Question 1, (3)

$$80,000 \times 1.15 = 92,000$$

92,000 blankets.

### Question 2, (2)

$$\begin{aligned} |p| &= \sqrt{6^2 + 27^2 + (-18)^2} \\ &= \sqrt{1089} \\ &= 33 \end{aligned}$$

### Question 3, (2)

$$\begin{aligned} \text{Area} &= \frac{1}{2} \times 45 \times 70 \times \sin 129^\circ \\ &= 1,224 \text{ cm}^2 \end{aligned}$$

### Question 4, (2)

$$\begin{aligned} &(3.6 \times 10^{-6}) \times 0.08 \\ &= 2.9 \times 10^{-7} \end{aligned}$$

### Question 5, (2)

$$A = (3, 0, 0)$$

$$B = (3, 3, 8)$$

### Question 6, (3)

$$3x^2 + 9x - 2 = 0$$

$$a = 3, b = 9, c = -2$$

$$\begin{aligned} x &= \frac{-9 \pm \sqrt{9^2 - 4(3)(-2)}}{2(3)} = \frac{-9 \pm \sqrt{81 + 24}}{6} \\ &= \frac{-9 \pm \sqrt{105}}{6} \end{aligned}$$



$$x = \frac{-9 + \sqrt{105}}{6} = 0.2 \text{ and } x = \frac{-9 - \sqrt{105}}{6} = -3.2$$

### Question 7, (3)

The smallest angle is at vertex Z.

Using the Cosine Rule gives

$$\begin{aligned} \cos Z &= \frac{8.5^2 + 7.2^2 - 6.3^2}{2(8.5)(7.2)} \\ &= \frac{84.4}{122.4} \end{aligned}$$

$$\begin{aligned} Z &= \cos^{-1}\left(\frac{84.4}{122.4}\right) \\ &= 46.4^\circ \end{aligned}$$

### Question 8, (5)

$$\begin{aligned} \text{Volume of hemi-sphere} &= \frac{1}{2} \times \frac{4}{3} \pi r^3 \\ &= \frac{1}{2} \times \frac{4}{3} \times \pi \times (12^3) \\ &= 3,619.11 \text{ cm}^3 \end{aligned}$$

$$\begin{aligned} \text{Volume of cylinder} &= \pi r^2 h \\ &= \pi \times (12^2) \times (70 - 12) \\ &= 26,238.58 \text{ cm}^3 \end{aligned}$$

$$\text{Volume of bollard} = 3,619.11 + 26,238.58 = 29,857.69 \text{ cm}^3$$

### Question 9, (3)

$$977.85 = 102.5\%$$

$$1\% = 977.85 \div 102.5 = 9.54$$

$$100\% = 9.54 \times 100 = 954$$

So, £954 is the price if she had paid on time.

$$£977.85 - £954 = £23.85$$

She could have saved £23.85.

**Question 10, (2)**

$$x^2 + 10x - 15 = (x + 5)^2 - 40$$

**Question 11, (4)**

The length of B to C is given by  $1500 - 600 - 650 = 250 \text{ m}$

$$650^2 = 422,500$$

$$600^2 + 250^2 = 422,500$$

Since  $600^2 + 250^2 = 650^2$  a triangle with short sides 600 & 250 and long side 650 is a right-angled triangle by the Converse of Pythagoras' Theorem.

$ABC$  is a right-angled triangle, meaning that B is due east of A since C is due north of B.

**Question 12, (3) (3)**

a) Linear Scale Factor =  $\frac{30}{50}$

$$\text{Area Scale Factor} = \left(\frac{30}{50}\right)^2 = 0.36$$

$$\text{Area} = 2,750 \times 0.36 = 990 \text{ cm}^2$$

b) Area =  $\frac{\text{angle}}{360} \times \pi r^2$

Let the angle  $ACB = x$

$$2,750 = \frac{x}{360} \times \pi \times 50^2$$

$$2,750 = \frac{2,500\pi x}{360}$$

$$x = \frac{2,750 \times 360}{2,500\pi}$$

$$x = 126.1^\circ$$

**Question 13, (3)**

$$\text{Gradient} = \frac{9 - 4p^2}{6 - 4p}$$

$$= \frac{(3 - 2p)(3 + 2p)}{2(3 - 2p)}$$

$$= \frac{3 + 2p}{2}$$



**Question 14, (3)**

$$5 \cos x + 2 = 1$$

$$5 \cos x = -1$$

$$\cos x = -\frac{1}{5}$$

$$\cos x = -0.2$$

$$\cos^{-1}(0.2) = 78^\circ$$

From CAST solutions lie in quadrants 2 & 3, giving

$$x = 180 - 78 = 102^\circ$$

$$x = 180 + 78 = 258^\circ$$

**Question 15, (3)**

$$\begin{aligned} \frac{4}{x-2} - \frac{3}{x+5} &= \frac{4(x+5)}{(x-2)(x+5)} - \frac{3(x-2)}{(x-2)(x+5)} \\ &= \frac{4(x+5) - 3(x-2)}{(x-2)(x+5)} \\ &= \frac{4x + 20 - 3x + 6}{(x-2)(x+5)} \\ &= \frac{x + 26}{(x-2)(x+5)} \end{aligned}$$

**Question 16, (3)**

$$\frac{a^4 x 3a}{\sqrt{a}} = \frac{3a^5}{a^{\frac{1}{2}}} = 3a^{5-\frac{1}{2}} = 3a^{\frac{9}{2}}$$

**Question 17, (2)**

$$\begin{aligned} (\sin x + \cos x)^2 &= (\sin x + \cos x)(\sin x + \cos x) \\ &= \sin^2 x + 2 \sin x \cos x + \cos^2 x \\ &= \sin^2 x + \cos^2 x + 2 \sin x \cos x \\ & \quad [\sin^2 x + \cos^2 x = 1 \text{ from Trig Identities}] \\ &= 2 \sin x \cos x + 1 \end{aligned}$$



### Question 18, (4)

Create a right angled triangle TSB

Since TS & SB are the radius of the circle they have length 7.5 cm

$$\begin{aligned}\text{By Pythagoras, } TB &= \sqrt{7.5^2 + 7.5^2} \\ &= 10.6 \text{ cm}\end{aligned}$$

TB is the radius of the larger circle, so TD also has length 10.6 cm

So, height = 10.6 + 15 = 25.6 cm.

### Question 19, (5)

$$\text{Angle } B = 180 - 52 - 34 = 94^\circ$$

Using the Sine Rule gives

$$\begin{aligned}\frac{b}{\sin B} &= \frac{k}{\sin K} = \frac{m}{\sin M} \\ \frac{350}{\sin 94^\circ} &= \frac{k}{\sin 52^\circ} = \frac{m}{\sin 34^\circ} \\ m &= \frac{350 \sin 34^\circ}{\sin 94^\circ} = 196 \text{ metres}\end{aligned}$$

Add a vertical line from B to the ground at point G to make a right-angled triangle BKG with angles 52°, 38°, 90°.

Using the Sine Rule gives

$$\begin{aligned}\frac{b}{\sin B} &= \frac{k}{\sin K} = \frac{g}{\sin G} \\ \frac{b}{\sin 38^\circ} &= \frac{k}{\sin 52^\circ} = \frac{196}{\sin 90^\circ} \\ k &= \frac{196 \sin 52^\circ}{\sin 90^\circ} = 154\end{aligned}$$

So, the height is 154 metres above the ground.